

<b>Tanta University</b>	<b>3<sup>rd</sup> year, Computers &amp; Control Dept.</b>
<b>Faculty of Engineering</b>	<b>Digital Control</b>

## Sheet 5

1. For the following open-loop Transfer functions:

i.  $\overline{GH}(z) = \frac{0.0952kz}{(z-1)(z-0.965)}$

ii.  $\overline{GH}(z) = \frac{z+0.9}{z(z-0.5)}$

iii.  $\overline{GH}(z) = \frac{z+1}{(1-z)^2}$

iv.  $\overline{GH}(z) = \frac{z}{(z^2-1)(z^2-z+0.5)}$

Calculate the steady-state error for input:

- a) A unit step
- b) A unit ramp
- c)  $r(t) = 3u(t) + 2t$

2. For the following open-loop Transfer functions:

i.  $\overline{GH}(z) = \frac{0.0952kz}{(z-1)(z-0.905)}$

ii.  $\overline{GH}(z) = \frac{k(z+0.9)}{(z-1)(z-0.7)}$

iii.  $\overline{GH}(z) = \frac{kz(z-0.5)}{(z-1)(z-0.8)}$

iv.  $\overline{GH}(z) = \frac{k(z-0.2)}{(z-1)(z+0.6)^2}$

v.  $\overline{GH}(z) = \frac{0.15k(z+0.7453)}{z(z-1)(z-0.4119)}$

- a) Draw the root locus
- b) Calculate the range of  $K$  for stability

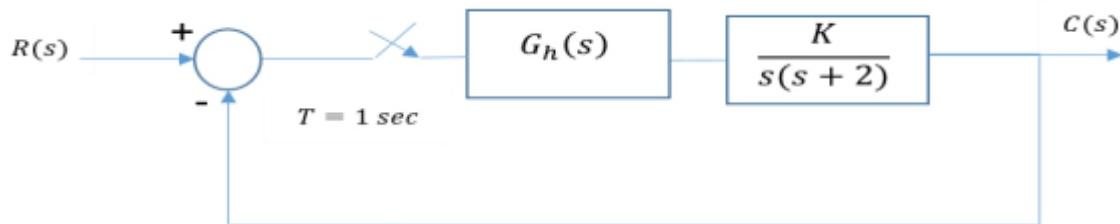
3. Consider the system given by:

$$\overline{GH}(z) = \frac{z + 1}{(1 - z)^2}$$

Assuming that the system is controlled by again controller ( $K$ ) in a unity feedback:

- a) Plot the root locus
- b) Can you stabilize this system with a gain controller?

4. Find using the root locus technique the stability range for the system shown in figure below.



5. Assume a unity feedback system with the transfer function

$$G(z) = Tz^{-1}(1 - z^{-1})$$

And a proportional control gain  $K$  show that instability results if  $KT > 0.5$ .